



--	--	--	--	--

--	--	--	--

0606/12

February/March 2019

2 hours

Additional Materials: Electronic calculator

READ THESE INSTRUCTIONS FIRST

DO **NOT** WRITE IN ANY BARCODES.

You are reminded of the need for clear presentation in your answers.

The total number of marks for this paper is 80.

This document consists of **15** printed pages and **1** blank page.

Mathematical Formulae**1. ALGEBRA***Quadratic Equation*

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1} b + \binom{n}{2} a^{n-2} b^2 + \dots + \binom{n}{r} a^{n-r} b^r + \dots + b^n,$$

where n is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

2. TRIGONOMETRY*Identities*

$$\sin^2 A + \cos^2 A = 1$$

$$\sec^2 A = 1 + \tan^2 A$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2} bc \sin A$$

1 (a) Given that $\mathcal{E} = \{x : 1 < x < 20\}$,

$$A = \{\text{multiples of } 3\},$$

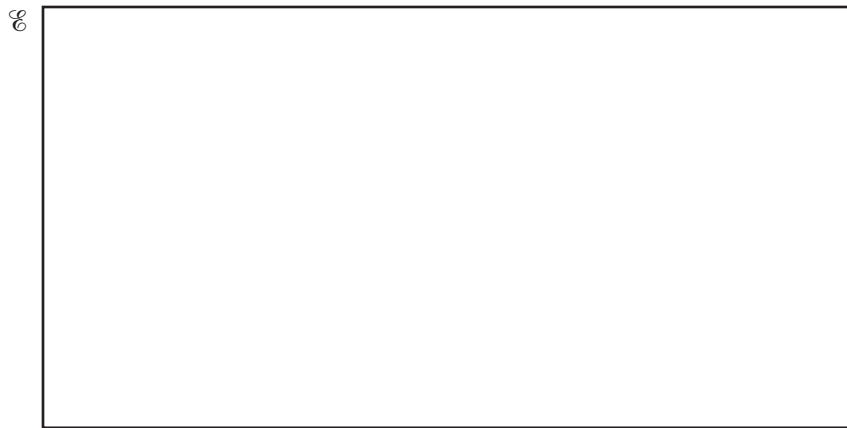
$$B = \{\text{multiples of } 4\},$$

find

(i) $n(A)$, [1]

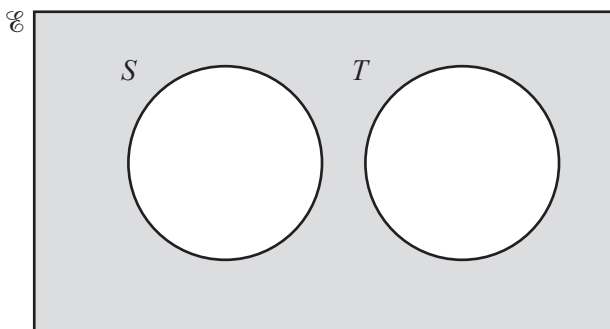
(ii) $n(A \cap B)$. [1]

(b) On the Venn diagram below, draw the sets P , Q and R such that $P \subset Q$ and $Q \cap R = \emptyset$.

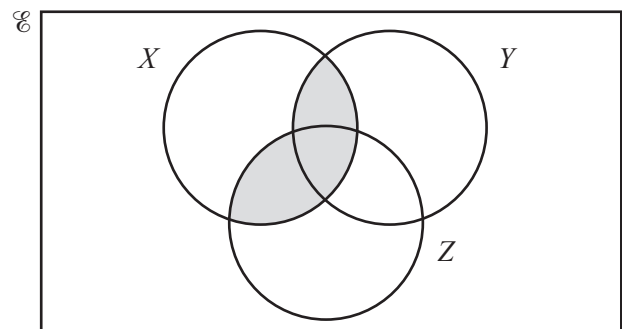


[2]

(c) Using set notation, describe the shaded areas shown in the Venn diagrams below.



.....



.....

[2]

- 2 On the axes below, sketch the graph of the curve $y = |2x^2 - 5x - 3|$, stating the coordinates of any points where the curve meets the coordinate axes.



[4]

- 3 (i) Find the first 3 terms in the expansion, in ascending powers of x , of $\left(3 - \frac{x}{9}\right)^6$. Give the terms in their simplest form. [3]

- (ii) Hence find the term independent of x in the expansion of $\left(3 - \frac{x}{9}\right)^6 \left(x - \frac{2}{x}\right)^2$. [3]

- 4 The polynomial $p(x) = 2x^3 + ax^2 + bx - 49$, where a and b are constants. When $p'(x)$ is divided by $x + 3$ there is a remainder of -24 .

(i) Show that $6a - b = 78$. [2]

It is given that $2x - 1$ is a factor of $p(x)$.

(ii) Find the value of a and of b . [4]

(iii) Write $p(x)$ in the form $(2x - 1)Q(x)$, where $Q(x)$ is a quadratic factor. [2]

(iv) Hence factorise $p(x)$ completely. [1]

5 It is given that $\log_4 x = p$. Giving your answer in its simplest form, find, in terms of p ,

(i) $\log_4(16x)$, [2]

(ii) $\log_4\left(\frac{x^7}{256}\right)$. [2]

Using your answers to **parts (i) and (ii)**,

(iii) solve $\log_4(16x) - \log_4\left(\frac{x^7}{256}\right) = 5$, giving your answer correct to 2 decimal places. [3]

- 6 (a) Given that $\mathbf{A} = \begin{pmatrix} 1 & 2 \\ 0 & -1 \end{pmatrix}$, $\mathbf{B} = \begin{pmatrix} 1 & -4 \\ 2 & 5 \\ 3 & 1 \end{pmatrix}$ and $\mathbf{C} = \begin{pmatrix} 3 & -2 & 0 \end{pmatrix}$, write down the matrix products which are possible. You do not need to evaluate your products. [2]

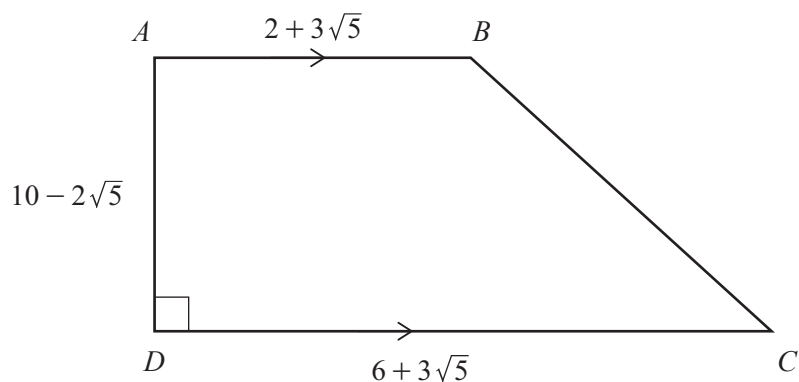
(b) It is given that $\mathbf{X} = \begin{pmatrix} 2 & -2 \\ 5 & 3 \end{pmatrix}$ and $\mathbf{Y} = \begin{pmatrix} 4 & 1 \\ 2 & 0 \end{pmatrix}$.

- (i) Find $\mathbf{X}^{-1}$. [2]

- (ii) Hence find the matrix $\mathbf{Z}$ such that $\mathbf{XZ} = \mathbf{Y}$. [3]

7 Do not use a calculator in this question.

All lengths in this question are in centimetres.

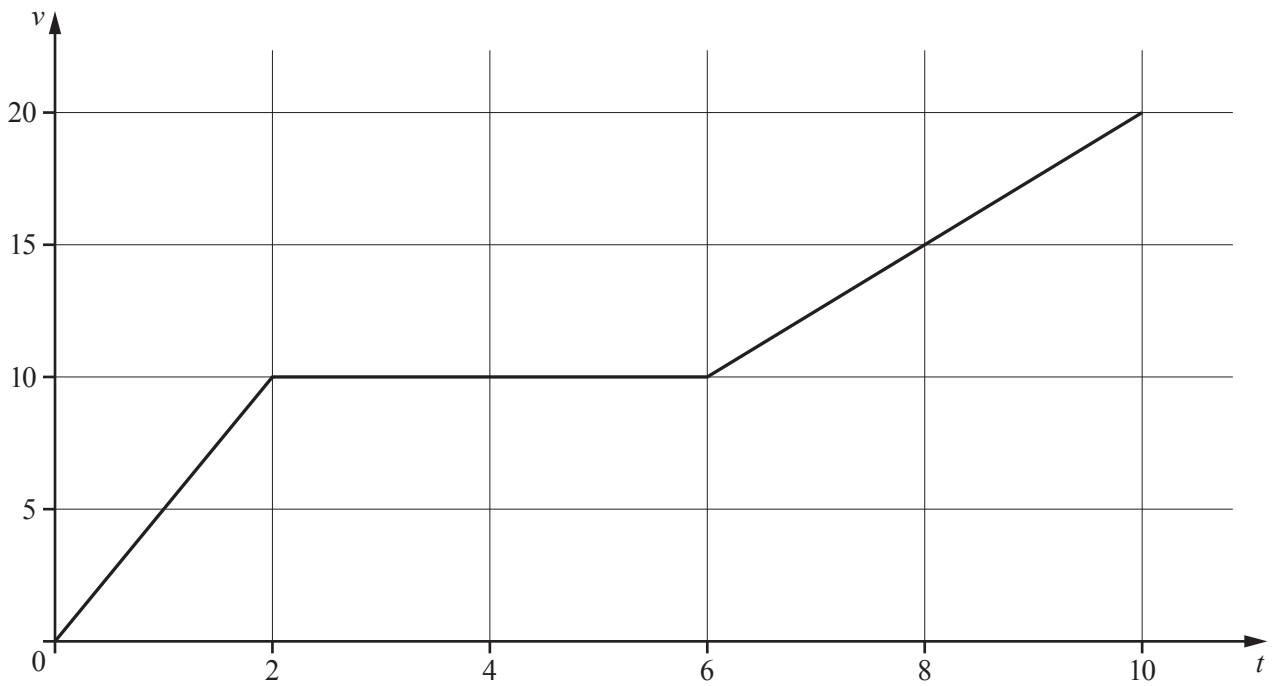


The diagram shows the trapezium $ABCD$, where $AB = 2 + 3\sqrt{5}$, $DC = 6 + 3\sqrt{5}$, $AD = 10 - 2\sqrt{5}$ and angle $ADC = 90^\circ$.

- (i) Find the area of $ABCD$, giving your answer in the form $a + b\sqrt{5}$, where a and b are integers. [3]

- (ii) Find $\cot BCD$, giving your answer in the form $c + d\sqrt{5}$, where c and d are fractions in their simplest form. [3]

8 (a)



The diagram shows the velocity-time graph of a particle P moving in a straight line with velocity $v \text{ ms}^{-1}$ at time t seconds after leaving a fixed point.

(i) Write down the value of the acceleration of P when $t = 5$. [1]

(ii) Find the distance travelled by the particle P between $t = 0$ and $t = 10$. [2]

(b) A particle Q moves such that its velocity, $v \text{ ms}^{-1}$, t seconds after leaving a fixed point, is given by $v = 3 \sin 2t - 1$.

(i) Find the speed of Q when $t = \frac{7\pi}{12}$. [2]

(ii) Find the least value of t for which the acceleration of Q is zero. [3]

9 The area of a sector of a circle of radius r cm is 36 cm^2 .

(i) Show that the perimeter, P cm, of the sector is such that $P = 2r + \frac{72}{r}$. [3]

(ii) Hence, given that r can vary, find the stationary value of P and determine its nature. [4]

10 A curve is such that when $x = 0$, both $y = -5$ and $\frac{dy}{dx} = 10$. Given that $\frac{d^2y}{dx^2} = 4e^{2x} + 3$, find

(i) the equation of the curve,

[7]

(ii) the equation of the normal to the curve at the point where $x = \frac{1}{4}$.

[3]

11 (a) Solve $\sin x \cos x = \frac{1}{2} \tan x$ for $0^\circ \leq x \leq 180^\circ$.

[3]

(b) (i) Show that $\sec \theta - \frac{\sin \theta}{\cot \theta} = \cos \theta$. [3]

(ii) Hence solve $\sec 3\theta - \frac{\sin 3\theta}{\cot 3\theta} = \frac{1}{2}$ for $-\frac{2\pi}{3} \leq \theta \leq \frac{2\pi}{3}$, where θ is in radians. [4]

BLANK PAGE

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge Assessment International Education Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cambridgeinternational.org after the live examination series.

Cambridge Assessment International Education is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of the University of Cambridge Local Examinations Syndicate (UCLES), which itself is a department of the University of Cambridge.