

--	--	--	--	--

--	--	--	--

0606/23

May/June 2017

2 hours

Additional Materials: Electronic calculator

READ THESE INSTRUCTIONS FIRST

DO **NOT** WRITE IN ANY BARCODES.

You are reminded of the need for clear presentation in your answers.

The total number of marks for this paper is 80.

This document consists of **15** printed pages and **1** blank page.

Mathematical Formulae**1. ALGEBRA***Quadratic Equation*

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1} b + \binom{n}{2} a^{n-2} b^2 + \dots + \binom{n}{r} a^{n-r} b^r + \dots + b^n,$$

where n is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

2. TRIGONOMETRY*Identities*

$$\sin^2 A + \cos^2 A = 1$$

$$\sec^2 A = 1 + \tan^2 A$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

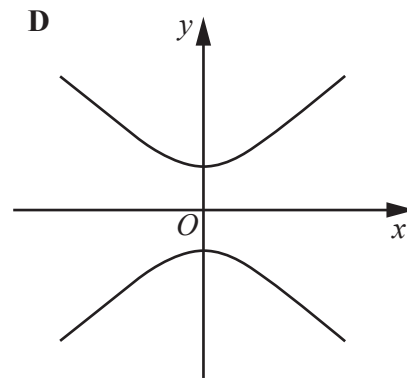
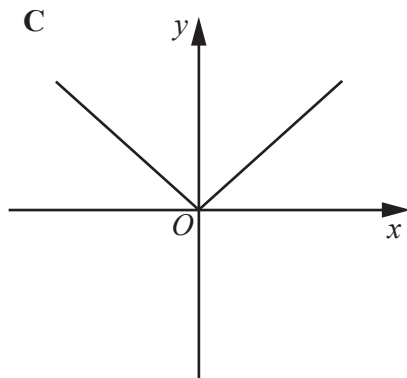
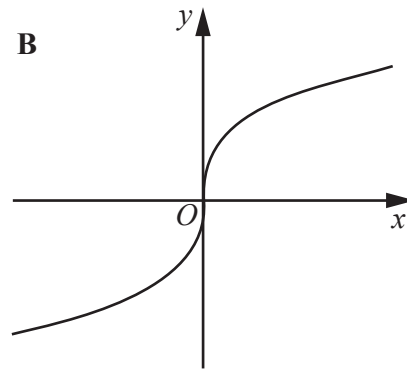
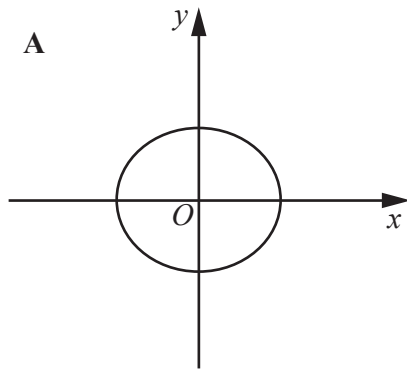
$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2} bc \sin A$$

- 1 (a) Solve the equation $7^{2x+5} = 2.5$, giving your answer correct to 2 decimal places. [3]

- (b) Express $\frac{(5\sqrt{q})^3}{(625p^{12}q)^{\frac{1}{4}}}$ in the form $5^a p^b q^c$, where a , b and c are constants. [3]

2

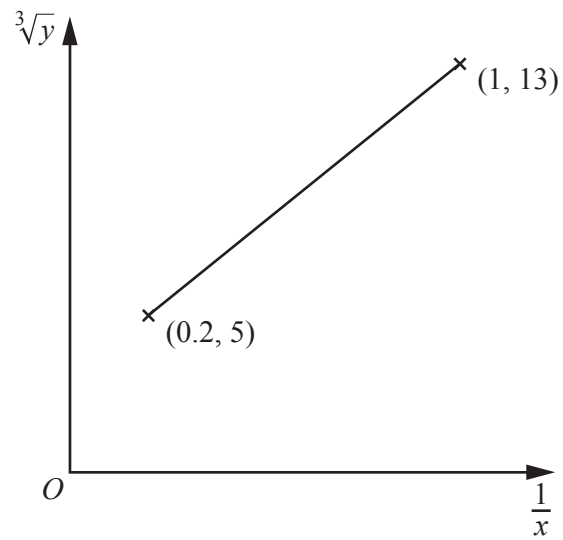


The four graphs above are labelled **A**, **B**, **C** and **D**.

(i) Write down the letter of each graph that represents a function, giving a reason for your choice. [2]

(ii) Write down the letter of each graph that represents a function which has an inverse, giving a reason for your choice. [2]

3



Variables x and y are such that when $\sqrt[3]{y}$ is plotted against $\frac{1}{x}$, a straight line graph passing through the points $(0.2, 5)$ and $(1, 13)$ is obtained. Express y in terms of x . [4]

- 4 (a) Vectors $\mathbf{a}$, $\mathbf{b}$ and $\mathbf{c}$ are such that $\mathbf{a} = \begin{pmatrix} 5 \\ -6 \end{pmatrix}$, $\mathbf{b} = \begin{pmatrix} 11 \\ -15 \end{pmatrix}$ and $3\mathbf{a} + \mathbf{c} = \mathbf{b}$.

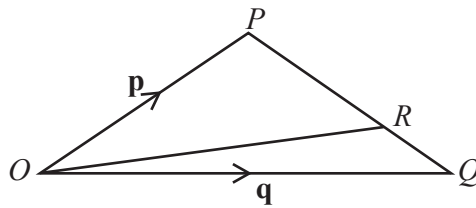
(i) Find $\mathbf{c}$.

[1]

(ii) Find the unit vector in the direction of $\mathbf{b}$.

[2]

(b)



In the diagram, $\vec{OP} = \mathbf{p}$ and $\vec{OQ} = \mathbf{q}$. The point R lies on PQ such that $PR = 3RQ$. Find $\vec{OR}$ in terms of $\mathbf{p}$ and $\mathbf{q}$, simplifying your answer.

[3]

5 (a) How many 5-digit numbers are there that have 5 different digits and are divisible by 5? [3]

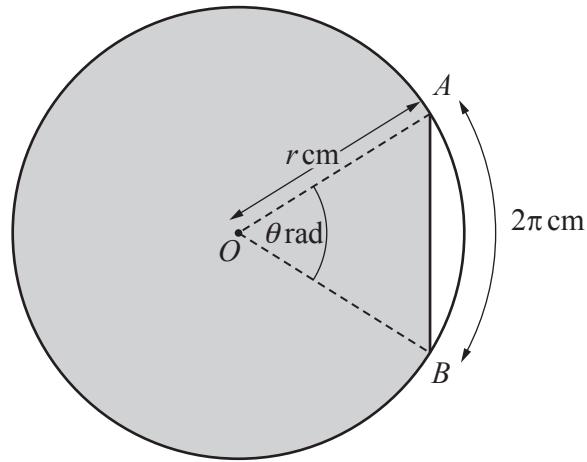
(b) A committee of 8 people is to be selected from 9 men and 5 women. Find the number of different committees that can be selected if the committee must have at least 4 women. [3]

- 6 The first three terms of the binomial expansion of $(2 - ax)^n$ are $64 - 16bx + 100bx^2$. Find the value of each of the integers n , a and b . [7]

7 Differentiate with respect to x ,

(i) $(1 + 4x)^{10} \cos x$, [4]

(ii) $\frac{e^{4x-5}}{\tan x}$. [4]



The diagram shows a circle, centre O of radius r cm, and a chord AB . Angle $AOB = \theta$ radians. The length of the major arc AB is 5 times the length of the minor arc AB . The minor arc AB has length 2π cm.

(i) Find the value of θ and of r . [2]

(ii) Calculate the exact perimeter of the shaded segment. [2]

(iii) Calculate the exact area of the shaded segment. [4]

- 9 The functions f and g are defined, for $x > 1$, by

$$\begin{aligned}f(x) &= 9\sqrt{x-1}, \\g(x) &= x^2 + 2.\end{aligned}$$

- (i) Find an expression for $f^{-1}(x)$, stating its domain. [3]

- (ii) Find the exact value of $fg(7)$. [2]

- (iii) Solve $gf(x) = 5x^2 + 83x - 95$. [4]

10 Solve the equation

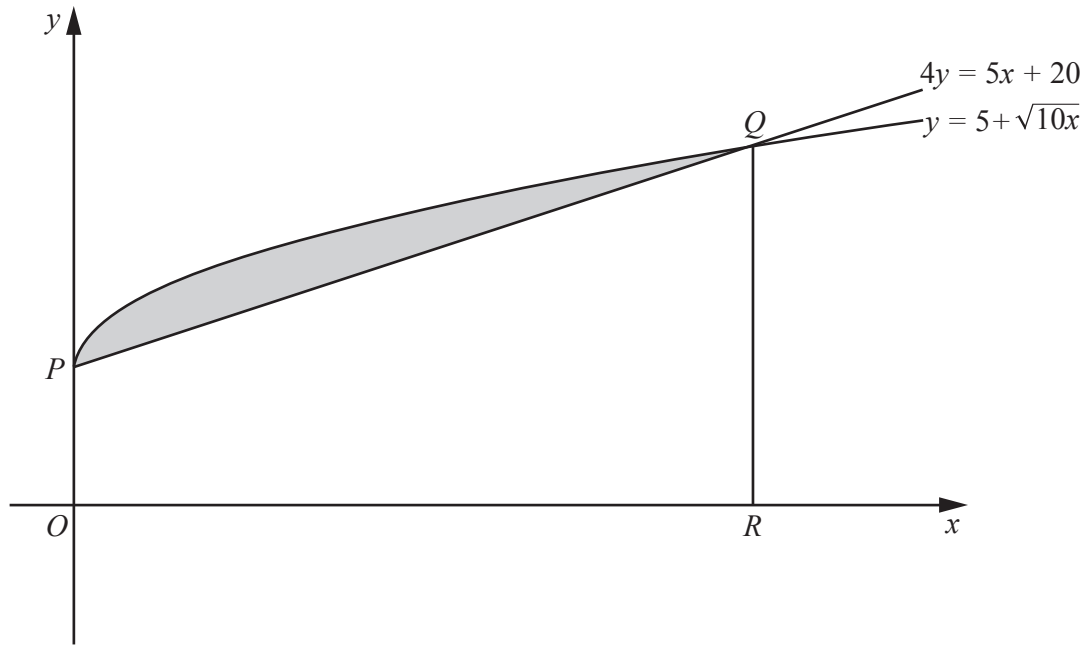
(a) $2|\sin x| = 1$ for $-\pi \leq x \leq \pi$ radians, [3]

(b) $3 \tan(2y + 15^\circ) = 1$ for $0^\circ \leq y \leq 180^\circ$, [4]

(c) $3 \cot^2 z = \operatorname{cosec}^2 z - 7 \operatorname{cosec} z + 1$ for $0^\circ \leq z \leq 360^\circ$.

[5]

11



The diagram shows part of the curve $y = 5 + \sqrt{10x}$ and the line $4y = 5x + 20$. The line and curve intersect at the points $P(0, 5)$ and Q . The line QR is parallel to the y -axis.

- (i) Find the coordinates of Q .

[4]

- (ii) Find the area of the shaded region. You must show all your working.

[6]

BLANK PAGE

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge International Examinations Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cie.org.uk after the live examination series.

Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.