

Cambridge International AS & A Level

FURTHER MATHEMATICS**9231/33**

Paper 3 Further Mechanics

May/June 2026**MARK SCHEME**Maximum Mark: 50

Published

This mark scheme contains the instructions and marking guidance that our examiners used to mark candidate responses for this component.

Before they start marking, examiners complete a standardisation process. They review a range of candidate responses and discuss the mark scheme in detail to agree which answers can and cannot be accepted. Examiners award marks where it is clear that candidate responses have met the requirements of the mark scheme. These requirements may vary between different components or different versions of the same component, depending on the exact requirements of the question and the candidate responses seen during the standardisation process.

Sometimes, our mark schemes may allow marks to be awarded to responses which contain elements that are factually incorrect or for content not covered by the syllabus. We do this in response to the demands of a specific question to support candidates and make sure that our assessments are fair. However, these allowances should not be used as a guide for teaching and learning.

We cannot discuss the mark scheme with schools, and we recommend that schools read the mark scheme together with the assessment material and the Principal Examiner Report for Teachers.

This document consists of **20** printed pages.

General marking principles

All examiners must apply these marking principles when marking candidate responses.

1	Examiners must award marks for each response in line with: - the specific content defined in the mark scheme - the specific skills defined in the mark scheme or in the level descriptions - the standard of response required as exemplified by the standardisation scripts.
2	Examiners must award whole marks (not half marks, or other fractions).
3	Examiners must award marks positively . This means that: - marks are not deducted for errors or omissions - marks are awarded for correct/valid answers as defined in the mark scheme and also for other valid answers which go beyond the scope of the syllabus and mark scheme referring to your team leader as appropriate - the quality of spelling, punctuation and grammar are judged only when the mark scheme indicates that these features are specifically assessed in the question. However, the meaning of all responses must be unambiguous.
4	Examiners must consistently apply the requirements of the mark scheme and any rules for what to do when candidates have not followed instructions correctly.
5	Examiners must use the full range of marks defined in the mark scheme, unless limited by the quality of the candidate responses seen.
6	Examiners must award marks according to the mark scheme and must not award marks with grade thresholds or grade descriptions in mind.

Mathematics Specific Marking Principles

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (ISW).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number or sign does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

Annotations guidance for centres

Examiners use a system of annotations as a shorthand for communicating their marking decisions to one another. Examiners are trained during the standardisation process on how and when to use annotations. The purpose of annotations is to inform the standardisation and monitoring processes and guide the supervising examiners when they are checking the work of examiners within their team. The meaning of annotations and how they are used is specific to each component and is understood by all examiners who mark the component.

We publish annotations in our mark schemes to help centres understand the annotations they may see on copies of scripts. Note that there may not be a direct correlation between the number of annotations on a script and the mark awarded. Similarly, the use of an annotation may not be an indication of the quality of the response.

The annotations listed below were available to examiners marking this component in this series.

Annotations

Annotation	Meaning
	More information required
	Accuracy mark awarded zero
	Accuracy mark awarded one
	Independent accuracy mark awarded zero
	Independent accuracy mark awarded one
	Independent accuracy mark awarded two
	Benefit of the doubt
	Blank Page
	Incorrect
Dep	Used to indicate DM0 or DM1

Annotation	Meaning
DM1	Dependent on the previous M1 mark(s)
	Follow through
	Indicate working that is right or wrong
Highlighter	Highlight a key point in the working
	Ignore subsequent work
	Judgement
	Judgement
	Method mark awarded zero
	Method mark awarded one
	Method mark awarded two
	Misread
	Omission or Other solution
Off-page comment	Allows comments to be entered at the bottom of the RM marking window and then displayed when the associated question item is navigated to.
On-page comment	Allows comments to be entered in speech bubbles on the candidate response.
	Judgment made by the PE
	Premature approximation
	Special case

Annotation	Meaning
	Indicates that work/page has been seen
	Error in number of significant figures
	Correct
	Transcription error
	Correct answer from incorrect working

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The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B** Mark for a correct result or statement independent of method marks.
- DM or DB** When a part of a question has two or more ‘method’ steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- FT** Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
 - For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
 - The total number of marks available for each question is shown at the bottom of the Marks column.
 - Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
 - Square brackets [] around text or numbers show extra information not needed for the mark to be awarded.

Abbreviations

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no ‘follow through’ from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

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Question	Answer	Marks	Guidance
1	$\uparrow R \cos \theta = mg$	B1	Resolve vertically.
	$\leftarrow R \sin \theta = m(a \sin \theta) \omega^2$	B1	Resolve horizontally. B1 for $R = ma \omega^2$ (with $\sin \theta$ cancelled). B0 for $R \sin \theta = mr \omega^2$ unless r replaced with $a \sin \theta$ later in working. B1 for $R \sin \theta = ma \frac{\sqrt{5}}{3} \omega^2$. Sight of $mg \tan \theta = m(a \sin \theta) \omega^2$ earns B1 B1 .
	$g = (a \cos \theta) \omega^2$ or $\omega^2 = \frac{g}{a \cos \theta}$ or $\cos \theta = \frac{g}{a \omega^2}$	M1	OE, eliminate R and m to get an expression in ω^2 . Must be obtained from equations with sin/cos mix only. $\tan \theta = \frac{\frac{1}{3} \sqrt{5} a \omega^2}{g}$
	$\frac{1}{3} a = a - a \cos \theta$, $\cos \theta = \frac{2}{3}$	B1	$\frac{1}{2} \sqrt{5} = \frac{\frac{1}{3} \sqrt{5} a \omega^2}{g}$
	$\omega = \sqrt{\frac{3g}{2a}}$	A1	OE, for example, $1.22 \sqrt{\frac{g}{a}}$.
		5	

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Question	Answer	Marks	Guidance
2	EITHER: $mv \frac{dv}{dx} = -k \frac{1}{x^2}$	(*B1)	N2L to form a differential equation in terms of $v \frac{dv}{dx}$. Accept $\pm k$. B0 for $mv \frac{dv}{dx} = -k \frac{1}{d^2}$.
	$\int mv dv = - \int \frac{k}{x^2} dx$ leading to $\frac{mv^2}{2} = \frac{k}{x} + c$	*M1	Separate variables correctly and integrate to obtain an equation of the form $mv^2 = \frac{\alpha}{x} (+c)$ where $\alpha \neq 0$. Condone omission of $+c$.
	$\left[\frac{\frac{1}{2}mv^2}{\frac{1}{2}mu^2} = \frac{1}{4} \right] \quad v^2 = \frac{1}{4}u^2 \quad \text{or} \quad v = \frac{1}{2}u$	*B1	Use kinetic energy loss to find v when $x = \frac{1}{2}d$. Implied by $x = \frac{1}{2}d$ and $v = \frac{1}{2}u$ as a boundary condition.
	$x=d, v=u \Rightarrow \frac{mu^2}{2} = \frac{k}{d} + c$ $x = \frac{1}{2}d, v = \frac{1}{2}u \Rightarrow \frac{mu^2}{8} = \frac{2k}{d} + c$	DM1	Use both sets of boundary conditions correctly to obtain two equations in c, k and d using <i>their</i> $\frac{mv^2}{2} = \frac{k}{x} + c$. Be aware k can be negative here, $k = \mp \frac{3}{8}mdu^2$. c may already have been found, $c = \pm \frac{7}{8}mu^2$. $\frac{1}{4} \left(\frac{k}{d} + c \right) = \frac{2k}{d} + c$ implies B1M1 .
	$0 = \frac{-\frac{3}{8}mdu^2}{x} + \frac{7mu^2}{8}$	DM1	Dependent on all marks so far. Substitute $v=0$. $c = -\frac{7k}{3d} \Rightarrow 0 = \frac{k}{d} - \frac{7k}{3d}$
	$\frac{3}{7}d$	A1)	SC B3 for correct answer if m is not present throughout.

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Question	Answer	Marks	Guidance
2	OR: Alternative method with x measured from A. $mv \frac{dv}{dx} = -k \frac{1}{(d-x)^2}$	(*B1)	N2L to form a differential equation in terms of $v \frac{dv}{dx}$. Accept $\pm k$.
	$\int mv dv = - \int \frac{k}{(d-x)^2} dx$ leading to $\frac{mv^2}{2} = -\frac{k}{(d-x)} + c$	*M1	Separate variables correctly and integrate to obtain an equation of the form $mv^2 = \frac{\alpha}{(d-x)} (+c)$ where $\alpha \neq 0$. Condone omission of $+c$.
	$\left[\frac{\frac{1}{2}mv^2}{\frac{1}{2}mu^2} = \frac{1}{4} \right] \quad v^2 = \frac{1}{4}u^2 \quad \text{or} \quad v = \frac{1}{2}u$	*B1	Use kinetic energy loss to find v when $x = \frac{1}{2}d$. Implied by $x = \frac{1}{2}d$ and $v = \frac{1}{2}u$ as a boundary condition.
	$x=0, v=u \Rightarrow \frac{mu^2}{2} = -\frac{k}{d} + c$ $x = \frac{1}{2}d, v = \frac{1}{2}u \Rightarrow \frac{mu^2}{8} = -\frac{k}{(d-\frac{1}{2}d)} + c$	DM1	Use both sets of boundary conditions correctly to obtain two equations in c, k and d using <i>their</i> $\frac{mv^2}{2} = -\frac{k}{(d-x)} + c$. Be aware k can be negative here, $k = \pm \frac{3}{8}mdu^2$. c may already have been found, $c = \pm \frac{7}{8}mu^2$.
	$0 = \frac{\frac{3}{8}mdu^2}{(d-x)} + \frac{7mu^2}{8}$	M1	Dependent on all marks so far. Substitute $v=0$.
	$x = \frac{4}{7}d$, minimum distance $= d - \frac{4}{7}d = \frac{3}{7}d$	A1)	SC B3 for correct answer if m is not present throughout.
	Available marks	6	

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Question	Answer	Marks	Guidance
3	At B, $mg \cos \beta = \frac{mv^2}{a}$	B1	N2L radially. If their equation contains R , only award this mark when R is set to 0.
	$\frac{1}{2}mv^2 - \frac{1}{2}mu^2 = mga(\cos \alpha - \cos \beta)$	*M1	Energy equation with 4 terms and correct dimensions (mass must be present). Allow sign errors and sin/cos mix only.
		A1	Fully correct energy equation.
	$ag \cos \beta - \left(\frac{2}{3}\right)^2 ag \cos \beta = 2ag(\cos \alpha - \cos \beta)$	DM1	Combine <i>their</i> two equations and substitute $u = \frac{2}{3}v$ to obtain an equation in, for example, $\cos \alpha$ and $\cos \beta$ only. Allow sin/cos mix only in <i>their</i> N2L equation radially. May, instead, see the following: $\cos \beta - \left(\frac{2}{3}\right)^2 \cos \beta = 2(\cos \alpha - \cos \beta)$ $\cos \beta - \frac{4}{9} \cos \beta = 2(\cos \alpha - \cos \beta)$
	$\cos \alpha : \cos \beta = 23 : 18$	A1	OE
		5	

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Question	Answer	Marks	Guidance															
4(a)	$\left(d^3 + \frac{1}{3}d^2h(k+1)\right)\bar{x} = \frac{1}{3}khd^2\left(\frac{1}{2}d + \frac{1}{4}kh\right)$	M1	Dimensionally correct moments equation, which must be of the form $\left(\alpha d^3 + \beta d^2h(k+1)\right)\bar{x} = khd^2\left(\gamma d + \delta kh\right)$ where $\alpha, \beta, \gamma, \delta$ are all non-zero constants. For reference:															
			<table><tr><td></td><td>Volume</td><td>From AB</td></tr><tr><td>Cube</td><td>d^3</td><td>0</td></tr><tr><td>Vertical pyramid</td><td>$\frac{1}{3}hd^2$</td><td>0</td></tr><tr><td>Horizontal pyramid</td><td>$\frac{1}{3}khd^2$</td><td>$\frac{1}{2}d + \frac{1}{4}kh$</td></tr><tr><td>Object</td><td>$d^3 + \frac{1}{3}d^2h(k+1)$</td><td>$\bar{x}$</td></tr></table>		Volume	From AB	Cube	d^3	0	Vertical pyramid	$\frac{1}{3}hd^2$	0	Horizontal pyramid	$\frac{1}{3}khd^2$	$\frac{1}{2}d + \frac{1}{4}kh$	Object	$d^3 + \frac{1}{3}d^2h(k+1)$	$\bar{x}$
				Volume	From AB													
			Cube	d^3	0													
			Vertical pyramid	$\frac{1}{3}hd^2$	0													
Horizontal pyramid	$\frac{1}{3}khd^2$	$\frac{1}{2}d + \frac{1}{4}kh$																
Object	$d^3 + \frac{1}{3}d^2h(k+1)$	$\bar{x}$																
B1	Either side of equation correct.																	
A1	Fully correct moments equation.																	
	$\bar{x} = \frac{kh(2d + kh)}{4(hk + h + 3d)}$	A1	OE, for example, $\frac{\frac{1}{3}khd^2\left(\frac{1}{2}d + \frac{1}{4}kh\right)}{d^3 + \frac{1}{3}d^2h(k+1)}$ or $\frac{2dkh + k^2h^2}{12d + 4kh + 4h}$. ISW															
		4																

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Question	Answer	Marks	Guidance
4(b)	$\bar{x} = \frac{1}{2}d$	B1FT	SOI, equate <i>their</i> $\bar{x}$ to $\frac{1}{2}d$.
	$k^2h^2 - 2dh - 6d^2 [=0]$	M1	Rearrange to obtain a 3-term quadratic in h of the form $\alpha k^2h^2 + \beta dh + \gamma d^2 [=0]$. Allow, for example, an equation of the form $k^2h^2 - 2dh = 6d^2$. <i>Their</i> $\bar{x}$ must be of the form $\frac{kh(\alpha d + \beta kh)}{(\gamma hk + \delta h + \epsilon d)}$, where $\alpha, \beta, \gamma, \delta, \epsilon$ are all non-zero constants
	$h = \frac{d + d\sqrt{1+6k^2}}{k^2} \left[= \frac{d}{k^2} \left(1 + \sqrt{1+6k^2} \right) \right]$	A1	OE, for example, $h = \frac{2d + \sqrt{4d^2 + 24k^2d^2}}{2k^2}$. If seen, must reject $\frac{d}{k^2} \left(1 - \sqrt{1+6k^2} \right)$.
		3	
4(c)	$1.5d = \frac{d}{k^2} \left(1 + \sqrt{1+6k^2} \right)$	M1	Dependent on M1 in 4(b). Equating <i>their</i> h to $1.5d$ or substituting $h = 1.5d$ into $k^2h^2 - 2dh - 6d^2 = 0$.
	$k = 2$ only	A1	If seen, $k = 0$ and $k = -2$ must be rejected.
		2	

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Question	Answer	Marks	Guidance
5(a)	$\frac{3}{5}u_A = \frac{4}{5}v_A$	*B1	Velocity perpendicular to line of centres. Substitute values of $\sin\alpha$ and $\sin\theta$. OE, for example, $3u_A = 4v_A$.
	$\left[\frac{\frac{1}{2}mu_A^2 - \frac{1}{2}m\left(\frac{3}{4}u_A\right)^2}{\frac{1}{2}mu_A^2} \times 100 = \right] 43.75 (\%)$	DB1	Calculate the percentage loss in KE of A. OE, for example, $\frac{175}{4}$. Condone 43.8.
		2	

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Question	Answer	Marks	Guidance
5(b)	$\frac{7}{25}u_B = \frac{3}{5}v_B \quad [7u_B = 15v_B]$	B1	Velocity perpendicular to line of centres. Values for trigonometric functions must be substituted.
	$mu_A \cos \alpha - mu_B \cos \beta = -mv_A \cos \theta + mv_B \cos \varphi$ leading to $m\left(\frac{4}{5}u_A\right) - m\left(\frac{24}{25}u_B\right) = -mv_A \times \frac{3}{5} + mv_B \times \frac{4}{5}.$	M1	Dimensionally correct momentum equation (m required). Allow sin/cos mix only. Values for trigonometric functions must be substituted. Allow 37 or better (36.8698...) for α, φ . Allow 16 or better (16.2602...) for β . Allow 53 or better (53.131...) for θ . OE, for example, $m\left(\frac{4}{5}u_A\right) - m\left(\frac{24}{25}u_B\right) = -m\left(\frac{3}{4}u_A\right) \times \frac{3}{5} + m\left(\frac{7}{15}u_B\right) \times \frac{4}{5}.$ May be implied by $15u_A = 16u_B, \quad 7v_A = 12v_B.$
	$e(u_A \cos \alpha + u_B \cos \beta) = v_A \cos \theta + v_B \cos \varphi$ leading to $e\left(\frac{4}{5}u_A + \frac{24}{25}u_B\right) = \frac{3}{5}v_A + \frac{4}{5}v_B$	M1	Use Newton's experimental law to form an equation. Allow sin/cos mix only. Values for trigonometric functions must be substituted. Allow 37 or better (36.8698...) for α, φ . Allow 16 or better (16.2602...) for β . Allow 53 or better (53.131...) for θ . Signs for approach velocities must be consistent with those for velocities before the collision in momentum equation. OE, for example, $e\left(\frac{4}{5}u_A + \frac{24}{25}u_B\right) = \frac{9}{20}u_A + \frac{28}{75}u_B.$
	$e = \frac{8}{17} [= 0.471]$	A1	Substitute expressions for u_A, v_A, u_B, v_B and simplify. $e = -\frac{88}{263} [= -0.335]$ from correct working B1M1M1A0 .
		4	

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Question	Answer	Marks	Guidance
6(a)	$T = \frac{1.6mgx}{10a}$	B1	Correct use of Hooke's law.
	$T = 0.2mg \times \frac{4}{5} [= 0.16mg]$	M1	Use of N2L, must be considering same mass on both sides. Allow sin/cos mix. Allow sign error. Must replace $\sin \theta$ with a numerical value.
	$0.16mg = \frac{1.6mgx}{10a}$ $x = a$ $OP = 10a - a = 9a.$	A1	AG , set up correct equation and find length.
		3	
6(b)	$\frac{1}{2} \times 0.3mv^2 = 10a \times \frac{4}{5} \times 0.3mg$ OR $v^2 = 2 \times 10a \times g \times \frac{4}{5}$	*M1	Energy equation before collision. Same mass on both sides (allow m instead of $0.3m$). Correct number of terms, dimensionally correct. Substitute value for $\sin \theta$ (may be done after m cancelled). Allow sin/cos mix. OR Use kinematics to find an equation containing v , a and g , including substituting value for $\sin \theta$. Allow sin/cos mix.
	$v = 4\sqrt{ag}$	A1	Award A1 for $v^2 = 16ag$.
	$0.3m \times 4\sqrt{ag} = (0.3m + 0.2m)w$	DM1	Dimensionally correct momentum equation, masses must be present, with <i>their</i> v substituted.
	$w = 2.4\sqrt{ag}$	A1	OE, for example, $\frac{1.2}{0.5}\sqrt{a}\sqrt{g}$. SC B1 for correct answer if m is missing throughout.
		4	

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Question	Answer	Marks	Guidance
6(c)	x defined as the distance from O (2 GPE terms): $\frac{1}{2} \times 0.5m \times "2.4^2 ag" + 0.5mg \times 9a \times \frac{4}{5} + \frac{1.6mga^2}{20a} = 0.5mg \times x \times \frac{4}{5} + \frac{1.6mg(10a-x)^2}{20a}$ OR x defined as the final extension (2 GPE terms): $\frac{1}{2} \times 0.5m \times "2.4^2 ag" + 0.5mg \times (x-a) \times \frac{4}{5} + \frac{1.6mga^2}{20a} = \frac{1.6mgx^2}{20a}$ OR x defined as the change in extension (one GPE term): $\frac{1}{2} \times 0.5m \times "2.4^2 ag" + 0.5mgx \times \frac{4}{5} + \frac{1.6mga^2}{20a} = \frac{1.6mg(x+a)^2}{20a}$	B1	At least one correct EPE.
		M1	Dimensionally correct energy equation with 2 EPE terms, one KE term and one/two GPE term(s) depending on how x is defined. Allow sign errors. Allow sin/cos mix. Values for trigonometric functions must be substituted. Allow slips in the EPE terms but must be of the form $k_1 x^2$. Do not allow sign errors in the EPE terms. Mass of particle needs to be present. Simplified equations for reference: $\frac{36}{25}mag + \frac{2}{5}mg(9a-x) + \frac{2mga^2}{25a} = \frac{2mg(10a-x)^2}{25a}$ OR $\frac{36}{25}mag + \frac{2}{5}mg(x-a) + \frac{2mga^2}{25a} = \frac{2mgx^2}{25a}$ OR $\frac{36}{25}mag + \frac{2}{5}mgx + \frac{2mga^2}{25a} = \frac{2mg(x+a)^2}{25a}$
		A1FT	All terms correct. FT <i>their</i> w^2 .
	$[x=]3a$	A1	If seen, must reject alternative solutions outside $[0, 10a]$.
		4	

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Question	Answer	Marks	Guidance
7(a)	$V_y = u_p \sin \alpha - gt$, and so $V_y = 25 \times \sin \alpha - 10t$.	B1	AG , minimum working $25 \times \frac{4}{5} - 10t = 0$ OR $\frac{25 \times \frac{4}{5}}{g} = \frac{20}{10}$. B0 if $20 - 10t = 0$ alone with no previous working shown. B0 if not using $g = 10$.
	At impact, $V_y = 0$, hence, $25 \times \frac{4}{5} - 10t = 0$, $t = 2$.		
		1	
7(b)	$h = 20 \times 2 - \frac{1}{2}g \times 2^2$	*M1	Use $s = ut + \frac{1}{2}at^2$ to find h . Substitute $t = 2$, $u = 25 \times \frac{4}{5}$ or $25 \times \frac{3}{5}$ and $a = \pm g$. May see $h = 25 \times \frac{4}{5} \times 2 \pm \frac{1}{2}g \times 2^2$ or $h = 25 \times \frac{3}{5} \times 2 \pm \frac{1}{2}g \times 2^2$ or $0 = 20^2 - 2gh$ or $h = \frac{20}{2} \times 2$. Must be clear that $h = 20$ is the maximum height.
	$25t_Q - \frac{1}{2}g \times t_Q^2 = '20'$	DM1	Use $s = ut + \frac{1}{2}at^2$ to find the time Q takes to get to h . Substitute $u = 25$ and $a = \pm g$. Allow <i>their</i> h . This line fully correct implies M1M1 .
	$t_Q = 1$, $T = 2 - t_Q = 1$	A1	Exclude $t_Q = 4$. Must distinguish between T and t_Q (for example, $t = 1$, $T = 1$ earns A1).
		3	

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Question	Answer	Marks	Guidance
7(c)	$v \cos \theta = u_P \cos \alpha [=15]$ leading to $v \sin \theta = \frac{15}{\cos \theta} \times \sin \theta$	*M1	Use the fact that horizontal component of the velocity is unchanged, meaning $v \cos \theta = 15$, to find the vertical component of the velocity of P after the collision, V_y . Implied by $V_y = 15 \tan \theta$.
	$[0 = (v \sin \theta)^2 - 2g \times y_{\max}]$ $0 = \left(\frac{15}{\cos \theta} \sin \theta \right)^2 - 2g \times y_{\max}$	DM1	Use $v^2 = u^2 + 2as$. Substitute <i>their</i> V_y and $a = \pm g$ with vertical component of velocity at maximum height set to 0 to find h .
	$y_{\max} = \frac{45}{4} \tan^2 \theta$	A1	
	Greatest height above ground $= 20 + \frac{45}{4} \tan^2 \theta$	A1	OE, for example, $20 + 11.25 \tan^2 \theta$.
		4	